

ProtoReg: Prototype Guidance and Dual-level Uncertainty-weighted Consistency for Semi-supervised Pulmonary Perfusion Regression

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Abstract. Pulmonary perfusion imaging is clinically important, but paired 3D CT-perfusion annotations are difficult to obtain. Semi-supervised learning (SSL) can exploit abundant unlabeled CT volumes, yet existing SSL methods are less effective for voxel-wise dense regression because continuous pseudo-labels lack reliable confidence estimates and strong consistency may amplify teacher noise. To address this, we propose ProtoReg, a semi-supervised framework for 3D non-contrast CT-to-perfusion regression with prototype-guided uncertainty modeling and sub-unit-aware learning. ProtoReg adopts a teacher-student framework with weak-to-strong consistency and maintains a learnable functional prototype bank to estimate uncertainty via prototype-induced entropy. Based on this uncertainty, we introduce a Dual-level Uncertainty-weighted Consistency Loss (DUW-CL), which re-weights consistency at both voxel and lung sub-unit levels to suppress noisy pseudo-label propagation. We further incorporate 1,000 external unlabeled CT volumes from public datasets to improve generalization without additional perfusion annotations. Experiments on two independent CT-perfusion cohorts show consistent improvements over strong SSL baselines, and ablations validate the effectiveness of prototype guidance, DUW-CL, and supervoxel-aware modeling. Code is publicly available at https://github.com/johnhamtom/ProtoReg_main.

Keywords: Lung imaging · Pulmonary perfusion · Semi-supervised learning · CT-to-SPECT regression · Consistency regularization · Uncertainty estimation.

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1 Introduction

Pulmonary perfusion maps reflect regional pulmonary blood flow and are essential for regional lung-function assessment, supporting the detection of pulmonary abnormalities and informing function-aware radiotherapy planning [13]. However, current acquisition techniques often require additional dedicated scans and rely on radioactive tracers or contrast agents, leading to increased cost, operational burden, and limited accessibility [7]. These practical limitations have motivated the exploration of deep learning-based surrogates that infer perfusion maps from routinely acquired chest CT.

Recent years have seen growing evidence that deep networks can infer lung SPECT-like perfusion from non-contrast chest CT, achieving moderate-to-high voxel-wise agreement with reference perfusion and suggesting that pulmonary parenchymal textures encode function-related cues for CT-to-perfusion translation [17, 16, 13]. Nevertheless, most existing methods still depend on sufficiently paired CT-perfusion data for supervised training or fine-tuning. In practice, paired acquisitions remain costly and scarce, whereas large-scale unlabeled CT scans are far more accessible, motivating semi-supervised learning under limited paired supervision.

Semi-supervised learning (SSL) has achieved remarkable success in image classification and segmentation [28, 15, 26]. Recent prototype- and uncertainty-based methods, including CPCL [23], UPCoL [14], and DyCON [4], further improve SSL by leveraging class-level prototypes, uncertainty estimates, or probability maps. However, these methods mainly rely on discrete category-level signals, whereas CT-to-perfusion regression requires reliability estimation for continuous voxel-wise pseudo-labels without direct confidence measures. Noisy pseudo-labels may then be reinforced by self-training or strong consistency regularization, leading to confirmation bias and unstable optimization [9, 2, 21].

This problem is especially challenging in lung functional imaging, where 3D perfusion patterns are heterogeneous and susceptible to motion-related inconsistencies [10]. Accordingly, SSL for pulmonary functional mapping is still in its infancy, with only limited recent work on adjacent directions [24]. Furthermore, relying solely on voxel-wise constraints may reinforce spatially fragmented pseudo-label noise, motivating the incorporation of sub-unit-level regional consistency [27, 29].

In this paper, we formulate 3D CT-to-perfusion synthesis as voxel-wise dense regression and propose ProtoReg, a teacher-student semi-supervised framework that learns from limited paired CT-perfusion scans together with large-scale unlabeled CT volumes. ProtoReg uses an EMA teacher to generate continuous pseudo-targets, and trains the student with a consistency objective under plausible CT perturbations, enabling effective utilization of unlabeled data for dense regression.

A central challenge in semi-supervised dense regression is pseudo-label confidence estimation: continuous voxel-wise targets lack a natural confidence score, and naive consistency can amplify noise. Motivated by prototype-based representation learning [5], we maintain a learnable functional prototype bank and

propose DUW-CL, a Dual-level Uncertainty-weighted Consistency loss. DUW-CL derives soft voxel-wise weights from prototype-induced entropy at voxel and lung sub-unit levels. Without hard filtering, all voxels are retained but assigned uncertainty-adaptive penalties: Early in training, the model focuses more on low-uncertainty regions at both voxel and sub-unit levels and tends to reduce the overall entropy; later, it shifts to refinement with milder entropy-guided weighting.

Overall, our contributions are fourfold: (1) We propose ProtoReg, a semi-supervised framework that integrates functional prototype guidance with uncertainty-aware optimization for accurate 3D lung perfusion estimation. (2) We introduce prototype-induced entropy as a reliability signal for continuous pseudo-targets, mitigating erroneous pseudo-label propagation in dense regression. (3) We propose DUW-CL, a Dual-level Uncertainty-weighted Consistency Loss that stabilizes training and promotes coherent functional patterns. (4) We demonstrate consistent gains on two independent CT-perfusion cohorts, with further improvements by incorporating external unlabeled CT volumes.

2 Method

2.1 Problem Setup

We study semi-supervised pulmonary perfusion synthesis from 3D non-contrast CT. The training set consists of a labeled set $\mathcal{D}_l = \{(x_i, y_i)\}_{i=1}^{N_l}$ and an unlabeled set $\mathcal{D}_u = \{x_j\}_{j=1}^{N_u}$, where x is a CT volume and y is the paired perfusion map (continuous-valued). We learn a voxel-wise regressor f_θ that outputs $\hat{y} = f_\theta(x)$. All voxel-wise losses are computed within the lung ROI Ω .

2.2 Overview of ProtoReg

An overview of ProtoReg is shown in Fig. 1. ProtoReg follows an EMA teacher-student paradigm with two networks of identical architecture: a student network f_θ and a teacher network $f_{\bar{\theta}}$. The teacher is updated by the exponential moving average (EMA) of the student at each iteration.

Labeled training. For labeled samples $(x_l, y_l) \in \mathcal{D}_l$, the student produces $\hat{y}_l = f_\theta(x_l)$ and is optimized by a supervised regression loss $\mathcal{L}_{sup} = \mathcal{L}_{sup}(\hat{y}_l, y_l)$ within Ω . Meanwhile, labeled perfusion maps provide reliable functional cues to update the prototype space: we quantize y_l into K functional bins and apply a prototype classification loss $\mathcal{L}_{proto}$ (Sec. 2.3) to train the prototype head and update the prototype bank.

Unlabeled training. For unlabeled samples $x_u \in \mathcal{D}_u$, we apply two augmentation strengths to obtain a weak view x_u^w and a strong view x_u^s . Then the student and teacher generate predictions:

$$\hat{y}_u^s = f_\theta(x_u^s), \quad \hat{y}_u^w = f_{\bar{\theta}}(x_u^w). \quad (1)$$

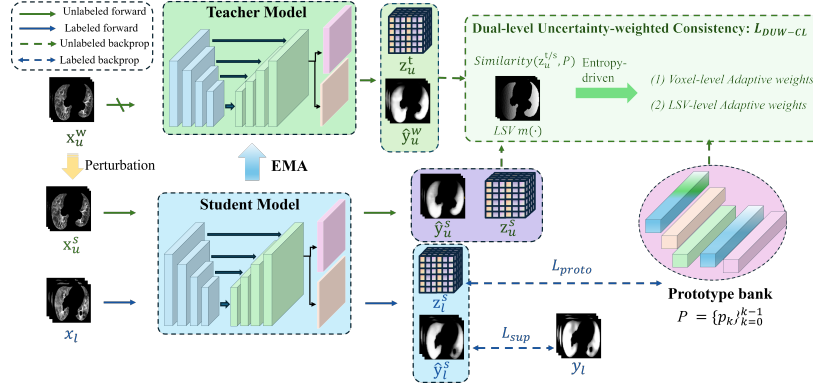


Fig. 1. Overview of the proposed ProtoReg framework.

We treat the teacher prediction $\hat{y}_u^w$ as the continuous pseudo target and enforce weak-to-strong consistency. Instead of confidence thresholding, we propose a Dual-level Uncertainty-weighted Consistency Loss (DUW-CL, Sec. 2.4), which estimates pseudo-label reliability via prototype-induced entropy and yields a voxel-wise reliability weight map $w(v)$ to suppress unreliable regions. The unlabeled objective is $\mathcal{L}_u = \mathcal{L}_{DUW-CL}$.

Overall objective and EMA update. The overall training objective is

$$\mathcal{L} = \underbrace{\mathcal{L}_{sup} + \lambda_{proto}\mathcal{L}_{proto}}_{\text{labeled}} + \underbrace{\mathcal{L}_{DUW-CL}}_{\text{unlabeled}}, \quad (2)$$

and the EMA update is $\bar{\theta} \leftarrow \alpha\bar{\theta} + (1 - \alpha)\theta$.

2.3 Prototype Update Strategy

We maintain a bank of K functional prototypes $\mathcal{P} = \{p_k\}_{k=0}^{K-1}$ to structure the voxel embedding space. Given a perfusion value $y(v)$, we first normalize it into a fixed range and then quantize it into K discrete bins. Each voxel v is thus assigned a bin index $c(v) \in \{0, \dots, K-1\}$ (from ground truth on labeled data).

For labeled samples $(x, y) \in \mathcal{D}_l$, the student network produces a voxel-wise embedding $z(v) \in \mathbb{R}^C$. We update the prototype space by encouraging $z(v)$ to be close to its assigned prototype $p_{c(v)}$. Specifically, we ℓ_2 -normalize both embeddings and prototypes and compute cosine-similarity logits

$$s_k(v) = \frac{\langle \tilde{z}(v), \tilde{p}_k \rangle}{\tau}, \quad k = 0, \dots, K-1, \quad (3)$$

where τ is a temperature scalar and $s(v) = [s_0(v), \dots, s_{K-1}(v)]$. The prototype update loss is defined as a cross-entropy classification objective over the K

prototypes:

$$\mathcal{L}_{proto} = \frac{1}{|\Omega|} \sum_{v \in \Omega} \text{CE}(\text{softmax}(s(v)), c(v)). \quad (4)$$

In practice, prototypes $\{p_k\}$ are implemented as learnable parameters and updated jointly with the student network via back-propagation. This loss refines $\mathcal{P}$ so that voxels with similar perfusion levels form compact, prototype-aligned clusters in the embedding space.

2.4 Dual-level Uncertainty-weighted Consistency Loss

Inspired by DyCON [4], we propose Dual-level Uncertainty-weighted Consistency Loss (DUW-CL) for unlabeled data, consisting of (i) a Dual-level Uncertainty-weighted Consistency term and (ii) a voxel-entropy regularizer. In this section, s and t denote student (on the strong view) and teacher (on the weak view), respectively.

Prototype-induced entropy. Let $z_s(v), z_t(v) \in \mathbb{R}^C$ be voxel-wise prototype embeddings and $\mathcal{P} = \{p_k\}_{k=0}^{K-1}$ the prototype bank (Sec. 2.3). We ℓ_2 -normalize embeddings/prototypes and compute cosine-similarity logits

$$s_{(\cdot)}^k(v) = \frac{\langle \tilde{z}_{(\cdot)}(v), \tilde{p}_k \rangle}{\tau}, \quad k = 0, \dots, K-1, \quad (5)$$

followed by assignment probabilities $q_{(\cdot)}(v) = \text{softmax}(s_{(\cdot)}(v))$ and entropy

$$H_{(\cdot)}(v) = - \sum_{k=0}^{K-1} q_{(\cdot)}^k(v) \log(q_{(\cdot)}^k(v) + \epsilon), \quad (\cdot) \in \{s, t\}. \quad (6)$$

(I) *Dual-level Uncertainty-weighted Consistency.* We partition the lung ROI Ω into M disjoint lung sub-units, implemented as lung supervoxels (LSV), and denote the sub-unit index of voxel v by $m(v) \in \{1, \dots, M\}$. We compute LSV mean-entropy maps by averaging entropy within each LSV and broadcasting the values back to voxels:

$$\bar{H}_{(\cdot)}(v) = \frac{1}{|\{u : m(u) = m(v)\}|} \sum_{u: m(u)=m(v)} H_{(\cdot)}(u). \quad (7)$$

Here, β_{vox} and β_{lsv} control entropy-weighting sharpness: larger values emphasize low-entropy predictions, while smaller values yield flatter weights. We then define voxel-/LSV-level denominators

$$\begin{aligned} d_{\text{vox}}(v) &= \exp(\beta_{\text{vox}} H_s(v)) + \exp(\beta_{\text{vox}} H_t(v)), \\ d_{\text{lsv}}(v) &= \exp(\beta_{\text{lsv}} \bar{H}_s(v)) + \exp(\beta_{\text{lsv}} \bar{H}_t(v)), \end{aligned} \quad (8)$$

and obtain the reliability weight

$$w(v) = \mathbf{1}_{\Omega}(v) \cdot \left((d_{\text{vox}}(v) + \epsilon)(d_{\text{lsv}}(v) + \epsilon) \right)^{-1}. \quad (9)$$

The normalized weighted consistency loss is

$$\mathcal{L}_{\text{cons}} = \frac{\sum_{v \in \Omega} w(v) \ell_{\text{reg}}(\hat{y}_s(v), \text{sg}(\hat{y}_w(v)))}{\sum_{v \in \Omega} w(v) + \epsilon}, \quad (10)$$

where $\text{sg}(\cdot)$ denotes stop-gradient, ℓ_{reg} is SmoothL1 loss. Following DyCON, we apply a geometric decay schedule $\beta(t) = \max\left(\beta_{\min}, \beta_{\max} \left(\frac{\beta_{\min}}{\beta_{\max}}\right)^{t/T}\right)$, and set $\beta_{\text{vox}} = \beta_{\text{lsv}} = \beta(t)$ unless stated otherwise.

(II) *Voxel entropy regularization and final loss.* We regularize prototype assignments by

$$\mathcal{L}_{\text{ent}} = \frac{1}{|\Omega|} \sum_{v \in \Omega} \frac{H_s(v) + H_t(v)}{2}, \quad (11)$$

which discourages overly diffuse assignments and mitigates a degenerate solution where the student increases entropy to down-weight $w(v)$, and define the final unlabeled loss

$$\mathcal{L}_{\text{DUW-CL}} = \lambda_{\text{cons}} \mathcal{L}_{\text{cons}} + \lambda_{\text{ent}} \mathcal{L}_{\text{ent}}. \quad (12)$$

3 Experiments

3.1 Experimental Settings

Datasets and pre-processing. We conduct experiments on two cohorts. Cohort A is a private hospital dataset of 233 PE-suspected patients from Queen Mary Hospital (2019–2023), approved by the Institutional Review Board (Approval No. UW 20-105; age: 65.5 ± 15.8 years; male: 39.4%). Cohort B is an access-controlled dataset of 100 thoracic CT studies with rigidly co-registered lung perfusion SPECT and lobe segmentations [1]. Each case contains paired 3D non-contrast CT and $^{99\text{m}}\text{Tc}$ -MAA SPECT. We also sample 1000 unlabeled CT volumes with axial slices $Z \geq 100$ from COVID19-CT-dataset [18], LIDC-IDRI [3], and MSD Task06_Lung [19]. For pre-processing, following [6], lung lobe masks were obtained using a pre-trained lobe segmentation model and merged as the lung ROI. Lung sub-units were generated by MaskSLIC [12] within each lobe at a target scale of 1 cm^3 . The original CT and SPECT volumes were approximately $512 \times 512 \times 200$ and 128^3 , respectively. Only the pre-segmented lung ROI was resampled/cropped to 128^3 to preserve CT–SPECT correspondence. CT intensities were clipped to $[-1000, 0]$ HU and linearly normalized, while SPECT was normalized by 1st/99th percentile stretching.

Training and evaluation. ProtoReg is implemented in PyTorch with a mean-teacher setup, where the student and EMA teacher ($\alpha = 0.996$) share a 3D U-Net [8] backbone and a lightweight prototype head with two $1 \times 1 \times 1$ convolutions. We use weak-to-strong consistency: both views share weak spatial transforms, while the student additionally receives intensity-only RandAugment

Table 1. Comparison on Cohort A.

Setting (L/U)	Method	Spearman $\rho \uparrow$	MAE $\downarrow$	SSIM $\uparrow$	FL20 $\uparrow$	FL40 $\uparrow$
100%/0%	Sup-only (3D U-Net)	0.780 $\pm$ 0.115	0.132 $\pm$ 0.032	0.758 $\pm$ 0.117	0.908 $\pm$ 0.072	0.817 $\pm$ 0.109
100%/1000CT	MT-Reg	0.786 $\pm$ 0.121	0.128 $\pm$ 0.035	0.768 $\pm$ 0.126	0.912 $\pm$ 0.071	0.823 $\pm$ 0.120
100%/1000CT	FixMatch-Reg	0.779 $\pm$ 0.128	0.133 $\pm$ 0.034	0.757 $\pm$ 0.129	0.905 $\pm$ 0.081	0.822 $\pm$ 0.115
100%/1000CT	UniMatch-Reg	0.772 $\pm$ 0.132	0.137 $\pm$ 0.032	0.741 $\pm$ 0.130	0.903 $\pm$ 0.084	0.818 $\pm$ 0.114
100%/1000CT	UniMatchV2-Reg	0.797 $\pm$ 0.100	0.126 $\pm$ 0.030	0.777 $\pm$ 0.099	0.912 $\pm$ 0.071	0.831 $\pm$ 0.105
100%/1000CT	ProtoReg	0.800$\pm$0.090	0.122$\pm$0.028*	0.781$\pm$0.092	0.913$\pm$0.072	0.834$\pm$0.102
20%/0%	Sup-only (3D U-Net)	0.765 $\pm$ 0.120	0.134 $\pm$ 0.032	0.750 $\pm$ 0.121	0.901 $\pm$ 0.071	0.797 $\pm$ 0.104
20%/80%	MT-Reg	0.776 $\pm$ 0.109	0.132 $\pm$ 0.032	0.758 $\pm$ 0.108	0.908 $\pm$ 0.070	0.816 $\pm$ 0.102
20%/80%	FixMatch-Reg	0.773 $\pm$ 0.125	0.136 $\pm$ 0.032	0.754 $\pm$ 0.122	0.901 $\pm$ 0.069	0.801 $\pm$ 0.098
20%/80%	UniMatch-Reg	0.776 $\pm$ 0.115	0.139 $\pm$ 0.030	0.752 $\pm$ 0.111	0.899 $\pm$ 0.071	0.803 $\pm$ 0.095
20%/80%	UniMatchV2-Reg	0.776 $\pm$ 0.110	0.133 $\pm$ 0.033	0.745 $\pm$ 0.115	0.903 $\pm$ 0.080	0.818 $\pm$ 0.110
20%/80%	ProtoReg	0.778$\pm$0.110	0.129$\pm$0.036*	0.764$\pm$0.118*	0.912$\pm$0.068*	0.822$\pm$0.105

* indicates significant improvement over UniMatchV2-Reg.

without geometric transforms ($N=2$ operations from noise/smoothing and intensity/histogram shifts). Models are trained for up to 500 epochs with Adam (batch size 1, lr 1×10^{-4} , wd 1×10^{-4}) and early stopping on the validation set. The supervised loss combines voxel-/LSV-level SmoothL1 and prototype update loss ($\lambda_{\text{proto}} = 0.01$). DUW-CL uses $\tau = 0.1$, $\lambda_{\text{cons}} = 1$, $\lambda_{\text{ent}} = 0.001$, and DyCON-style geometric decay with $\beta_{\text{max}} = 5$, $\beta_{\text{min}} = 0.5$, and $T = 10,000$.

All metrics are computed within the lung ROI Ω and reported as per-case mean $\pm$ standard deviation on the test set. We evaluate MAE, SSIM, Spearman’s ρ , and functional-lung overlap indices FL20/FL40 [11]. For $x \in \{0.2, 0.4\}$, $R_x = \{v \in \Omega \mid y(v) \geq x \max_{u \in \Omega} y(u)\}$ and $\hat{R}_x = \{v \in \Omega \mid \hat{y}(v) \geq x \max_{u \in \Omega} \hat{y}(u)\}$; $\text{FL}x = \text{Dice}(\hat{R}_x, R_x)$.

3.2 Results and Visualizations

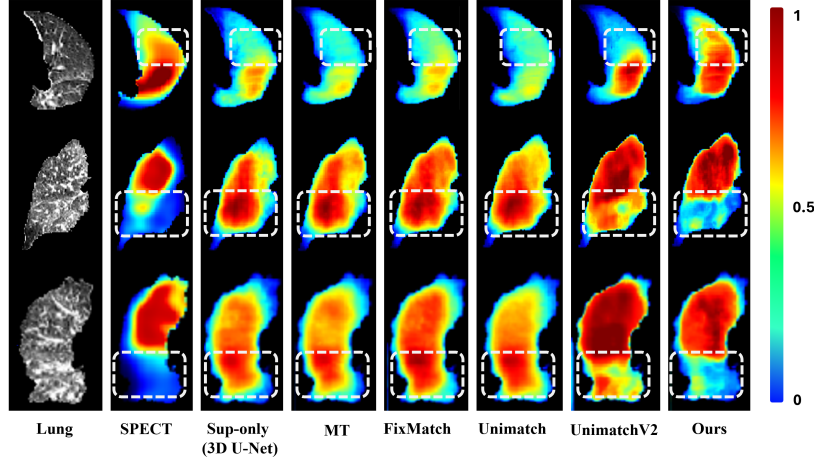
Comparison with Baselines Since no prior SSL method is tailored to 3D CT-to-perfusion regression, we adapt representative, transferable SSL baselines for dense prediction—Mean Teacher [22] and FixMatch [20]/UniMatch-style [25, 26] consistency learning—resulting in MT-Reg, FixMatch-Reg, UniMatch-Reg, and UniMatchV2-Reg. All methods share the same 3D U-Net backbone, splits, pre-processing, augmentations, evaluation protocol, and major hyperparameters for fair comparison. As shown in Table 1 and Table 2, ProtoReg consistently achieves best or comparable performance on both Cohort A and Cohort B under two SSL settings (fixed 80/20 train–test split): in-domain SSL (20% labeled + in-domain unlabeled CT) and external-unlabeled SSL (100% labeled + 1000 external unlabeled CT). On Cohort B with full labels, generic SSL baselines can underperform Sup-only, likely due to external-domain mismatch or noisy pseudo-targets; ProtoReg remains more robust. Representative visualizations are shown in Fig. 2.

Ablation Studies We conduct ablations on Cohort A under the 20% labeled setting (Table 3). A moderate prototype granularity performs best. Replacing our uncertainty re-weighting with fixed-threshold filtering based on the teacher’s prototype-assignment probability (max prototype similarity probability $> 0.90 / 0.95$) consistently underperforms, suggesting hard filtering is suboptimal for

Table 2. Comparison on Cohort B.

Setting (L/U)	Method	Spearman $\rho \uparrow$	MAE $\downarrow$	SSIM $\uparrow$	FL20 $\uparrow$	FL40 $\uparrow$
100%/0%	Sup-only (3D U-Net)	0.810 $\pm$ 0.091	0.119$\pm$0.026	0.792 $\pm$ 0.091	0.872 $\pm$ 0.053	0.796 $\pm$ 0.066
100%/1000CT	MT-Reg	0.802 $\pm$ 0.087	0.122 $\pm$ 0.025	0.786 $\pm$ 0.089	0.868 $\pm$ 0.053	0.790 $\pm$ 0.068
100%/1000CT	FixMatch-Reg	0.797 $\pm$ 0.078	0.126 $\pm$ 0.024	0.767 $\pm$ 0.081	0.865 $\pm$ 0.056	0.787 $\pm$ 0.069
100%/1000CT	UniMatch-Reg	0.801 $\pm$ 0.089	0.126 $\pm$ 0.026	0.774 $\pm$ 0.088	0.864 $\pm$ 0.055	0.773 $\pm$ 0.071
100%/1000CT	UniMatchV2-Reg	0.806 $\pm$ 0.082	0.123 $\pm$ 0.025	0.780 $\pm$ 0.091	0.871 $\pm$ 0.051	0.794 $\pm$ 0.065
100%/1000CT	ProtoReg	0.814$\pm$0.077*	0.119 $\pm$ 0.026*	0.799$\pm$0.085*	0.873$\pm$0.050	0.798$\pm$0.065
20%/0%	Sup-only (3D U-Net)	0.740 $\pm$ 0.085	0.147 $\pm$ 0.023	0.702 $\pm$ 0.091	0.846 $\pm$ 0.050	0.735 $\pm$ 0.064
20%/80%	MT-Reg	0.759 $\pm$ 0.083	0.146 $\pm$ 0.029	0.723 $\pm$ 0.098	0.857 $\pm$ 0.053	0.757 $\pm$ 0.064
20%/80%	FixMatch-Reg	0.767 $\pm$ 0.075	0.139 $\pm$ 0.026	0.730 $\pm$ 0.087	0.862$\pm$0.053	0.764 $\pm$ 0.065
20%/80%	UniMatch-Reg	0.749 $\pm$ 0.091	0.145 $\pm$ 0.032	0.718 $\pm$ 0.114	0.854 $\pm$ 0.050	0.758 $\pm$ 0.077
20%/80%	UniMatchV2-Reg	0.758 $\pm$ 0.087	0.145 $\pm$ 0.029	0.722 $\pm$ 0.105	0.856 $\pm$ 0.049	0.753 $\pm$ 0.072
20%/80%	ProtoReg	0.769$\pm$0.102*	0.138$\pm$0.027*	0.739$\pm$0.109*	0.861 $\pm$ 0.048	0.767$\pm$0.066*

* indicates significant improvement over UniMatchV2-Reg.

**Fig. 2.** Qualitative comparisons on CT-to-perfusion SPECT regression.**Table 3.** Ablation studies on Cohort A under the 20% labeled setting.

Variant	Spearman $\rho \uparrow$	MAE $\downarrow$	SSIM $\uparrow$	FL20 $\uparrow$	FL40 $\uparrow$
<i>(A) Number of prototype bins K</i>					
$K = 2$	0.773 $\pm$ 0.110	0.132 $\pm$ 0.037	0.757 $\pm$ 0.112	0.910 $\pm$ 0.072	0.821 $\pm$ 0.107
$K = 5$	0.778$\pm$0.110	0.129$\pm$0.036	0.764$\pm$0.118	0.912$\pm$0.068	0.822$\pm$0.105
$K = 10$	0.766 $\pm$ 0.105	0.133 $\pm$ 0.034	0.753 $\pm$ 0.107	0.908 $\pm$ 0.068	0.819 $\pm$ 0.102
<i>(B) DUW-CL design choices</i>					
th_consist=0.90	0.767 $\pm$ 0.113	0.135 $\pm$ 0.031	0.747 $\pm$ 0.108	0.902 $\pm$ 0.069	0.816 $\pm$ 0.099
th_consist=0.95	0.773 $\pm$ 0.119	0.133 $\pm$ 0.033	0.751 $\pm$ 0.117	0.904 $\pm$ 0.071	0.820 $\pm$ 0.110
only voxel (w/o LSV)	0.774 $\pm$ 0.105	0.132 $\pm$ 0.037	0.758 $\pm$ 0.112	0.909 $\pm$ 0.072	0.823$\pm$0.106
ours (voxel+LSV)	0.778$\pm$0.110	0.129$\pm$0.036*	0.764$\pm$0.118*	0.912$\pm$0.068*	0.822 $\pm$ 0.105

* indicates significant improvement over voxel-only (w/o LSV).

dense regression with continuous pseudo targets. Finally, removing the LSV-level weighting (“only voxel”) degrades MAE, SSIM, FL20, validating the benefit of regional uncertainty in the full voxel+LSV design.

4 Conclusion

In this paper, we propose ProtoReg, a teacher–student semi-supervised framework for 3D non-contrast CT-to-perfusion regression with limited paired data. It leverages a learnable functional prototype bank to compute prototype-induced entropy for voxel-wise uncertainty, and proposes DUW-CL, a Dual-level Uncertainty-weighted Consistency loss that suppresses noisy pseudo-labels and promotes anatomically coherent patterns. Experiments on two independent cohorts show consistent gains in correlation, reconstruction quality, and high-functional indicators, and remain effective when incorporating 1,000 external unlabeled CTs. Future work will extend to multi-center generalization, additional functional targets, and more robust sub-unit modeling and uncertainty calibration.

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