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# TOF-GR: Unsupervised PET Reconstruction via Time-of-Flight Gaussian Representation and Kernel-Based Prior Modeling

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**Abstract.** PET reconstruction is inherently ill-posed due to the extremely low signal-to-noise ratio (SNR) of raw projection data. Although supervised deep learning has achieved superior results in low-count scenarios, its clinical adoption is hindered by the reliance on high-quality paired datasets and limited generalization. While self-supervised Implicit Neural Representations (INRs) show promise for PET reconstruction, their inherent spectral bias causes MLPs to overfit high-frequency noise, yielding artifacts or over-smoothing. We propose a self-supervised framework that transforms the PET reconstruction paradigm toward explicit 3D Gaussian Splatting (3DGS). By representing the radioactivity image as a collection of controllable and anisotropic Gaussian primitives, our method effectively decouples local signal recovery from global noise propagation. We develop a differentiable pipeline incorporating the PET system matrix into Gaussian voxelization. To enhance image fidelity, we introduce a framework integrating Gaussian representation with kernel method, where a kernel matrix derived from MRI priors is incorporated into the voxelization stage. Experiments on brain and thorax datasets demonstrate that our method outperforms traditional iterative algorithms and state-of-the-art self-supervised approaches. By establishing a novel explicit representation for PET, this work provides a robust and interpretable solution for low-SNR clinical scenarios.

**Keywords:** PET Reconstruction · 3D Gaussian Representation · Kernel Method.

## 1 Introduction

Positron emission tomography (PET) provides critical functional information for tumor staging by tracking in vivo metabolic activities [26]. However, the

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cumulative risks of ionizing radiation have compelled a clinical imaging transition toward low-dose scenarios [21]. Limited by photon starvation, low-dose reconstruction evolves into a highly ill-posed inverse problem, compromising the accurate restoration of sub-centimeter lesions.

To bolster SNR, conventional PET denoising encompasses three distinct strategies. Sinogram filtering prior to FBP induces resolution degradation due to inherent photon sparsity. Iterative optimization, notably MLEM [23] and Maximum A Posteriori (MAP) [12], incorporates structural regularizations into the objective function. Despite sharpening boundaries, excessive iterations or ill-tuned hyperparameters inevitably exacerbate Poisson noise and computational overhead. Image-space algorithms (e.g., BM3D [5], NLM [3]) operate independently of projection data to suppress artifacts, yet their robust denoising proficiency often triggers over-smoothing, systematically obliterating sub-centimeter anatomical configurations.

While deep learning techniques [22, 28] covering from end-to-end direct reconstruction [9] to physics-driven unrolled networks [1, 8] transcend traditional bottlenecks, they rely heavily on large-scale and high-fidelity paired clinical data which is impractical to acquire. Thus, unsupervised paradigms have emerged. Early hand-crafted priors such as total variation (TV) or low-rank sparsity [27] often suffer from over-smoothing. Subsequently, Kernel Methods [7, 13, 14] guided by high-resolution anatomical priors significantly enhanced structural fidelity. Although Deep Image Prior (DIP) [25] exploits CNNs for denoising, its inherent low-pass filtering prioritizes convergence toward low-frequency backgrounds, blurring lesion edges during early optimization stages [7, 16]. Furthermore, while MLP-based Implicit Neural Representations (INRs) [18] facilitate continuous modeling, they face severe spectral bias [24]. Under strong Poisson noise, their globally coupled mapping easily triggers gradient oscillations, leading to distorted lesion boundaries and prohibitive computational costs [19].

To overcome the representational bottlenecks of implicit networks, 3D Gaussian Splatting (3DGS) [11] has recently emerged as a promising alternative, demonstrating superior detail recovery and computational efficiency compared to NeRFs. By explicitly parameterizing the volume with a set of anisotropic Gaussian kernels, 3DGS facilitates high-frequency structural representation. Consequently, this paradigm has been introduced into the medical imaging domain with promising preliminary attempts, successfully achieving reconstructions in sparse-view CT [15, 29], undersampled MRI [20], and demonstrating superior spatiotemporal detail recovery in dynamic CBCT [4, 10] and vessel reconstruction [17, 30]. However, its application in PET remains largely unexplored. Especially in low-dose scenarios, unconstrained Gaussian representations are prone to overfitting Poisson noise due to the lack of regularization, resulting in morphological collapse and artifacts.

In this study, we propose an unsupervised, multimodal image-guided Gaussian reconstruction framework designed to confine Gaussian primitives within an anatomically plausible manifold. Unlike generative schemes that rely on pre-trained diffusion models [6], our approach is physics-driven and completely cir-

cumvents the need for external pre-trained models. The contributions of our work are as follows:

1. TOF-weighted explicit Gaussian representation: TOF-weighted GS is developed for unsupervised PET reconstruction, capitalizing on explicit local parameterization to precisely capture sub-centimeter lesion details.

2. Anatomical manifold constraint: We propose a kernel regularization strategy guided by multimodal prior images to ensure morphological fidelity.

3. Physics-Consistent Optimization: We formulate a synergistic optimization objective integrating Poisson likelihood with TV penalty, enabling highly efficient and stable convergence under extreme low-count conditions.

## 2 Method

### 2.1 PET Gaussian Representation

As shown in Fig.1, we parameterize the continuous radiotracer distribution using a set of learnable 3D Gaussian primitives. Let  $\Theta = \{\boldsymbol{\mu}_g, \boldsymbol{\Sigma}_g, \alpha_g\}_{g=1}^{N_g}$  denote the collective attributes of  $N_g$  Gaussian kernels, where  $\boldsymbol{\mu}_g \in \mathbb{R}^3$ ,  $\boldsymbol{\Sigma}_g \in \mathbb{R}^{3 \times 3}$ , and  $\alpha_g \in \mathbb{R}^+$  represent the spatial center, covariance matrix, and intensity coefficient, respectively. The tracer activity at any spatial coordinate  $\mathbf{r}_i \in \mathbb{R}^3$  is formulated as the cumulative response of its local Gaussian primitives:

$$x(\mathbf{r}_i|\Theta) = \sum_{g=1}^{N_g} \alpha_g \exp\left(-\frac{1}{2}(\mathbf{r}_i - \boldsymbol{\mu}_g)^\top \boldsymbol{\Sigma}_g^{-1}(\mathbf{r}_i - \boldsymbol{\mu}_g)\right) \quad (1)$$

To enable anisotropic spatial adaptivity for complex anatomical structures,  $\boldsymbol{\Sigma}_g$  is derived from a learnable scaling vector  $\mathbf{s}_g \in \mathbb{R}^3$  and rotation quaternion  $\mathbf{q}_g \in \mathbb{R}^4$ . These can be transformed into a diagonal scaling matrix  $\mathbf{S}_g \in \mathbb{R}^{3 \times 3}$  and a rotation matrix  $\mathbf{R}_g \in \mathbb{R}^{3 \times 3}$ , such that:

$$\boldsymbol{\Sigma}_g = \mathbf{R}_g \mathbf{S}_g \mathbf{S}_g^\top \mathbf{R}_g^\top \quad (2)$$

By integrating this continuous representation into the physical Time-of-Flight (TOF) PET forward model, the expected projection data expands into a TOF sinogram  $\bar{\mathbf{y}} \in \mathbb{R}^{M \times T}$ , where  $M$  is the number of Lines of Response (LORs) and  $T$  is the number of TOF bins. The expectation for the  $m$ -th LOR and  $t$ -th TOF bin,  $\bar{y}_{m,t}$ , is directly formulated as:

$$\bar{y}_{m,t} = \sum_{i=1}^N P_{m,i} h(t - \Delta t_{m,i}) x(\mathbf{r}_i|\Theta) + n_{m,t}$$

Alternatively, this can be expressed in compact matrix notation as:

$$\bar{\mathbf{y}} = \mathbf{P}_{\text{TOF}} \cdot \mathbf{x}(\Theta) + \mathbf{n} \quad (3)$$

where  $\mathbf{P}_{\text{TOF}} \in \mathbb{R}^{MT \times N}$  is the combined spatio-temporal system matrix. The

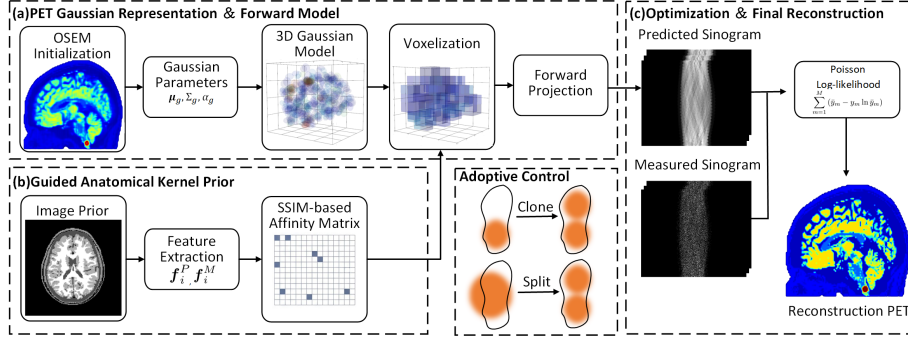


Fig. 1: The overall framework of the proposed anatomically-guided 3D Gaussian PET reconstruction. (a) Parameter initialization derived from the OSEM reconstruction, followed by voxelization and forward projection to acquire the predicted sinogram. (b) Extraction of anatomical priors from MRI/CT images to construct the  $K$  matrix. (c) Optimization of the Gaussian parameters using Poisson loss.

spatial component  $P_{m,i}$  incorporates detection geometry, attenuation, and normalization. The function  $h(\cdot)$  represents the detector TOF profile, typically modeled as a 1D Gaussian corresponding to the system’s temporal resolution, and  $\Delta t_{m,i}$  denotes the expected photon arrival time difference for an emission at spatial coordinate  $\mathbf{r}_i$  along LOR  $m$ . Finally,  $\mathbf{n}$  accounts for the TOF-distributed random and scattered events.

**Tractable Optimization Strategy.** To facilitate tractable optimization of the Gaussian representation, we implement a tripartite strategy: (i) Rapid voxelization. We employ a rapid voxelization strategy introduced by [29] to bridge the continuous Gaussian parameterization with the discrete system matrix  $\mathbf{P}$ . (ii) Initialization. To prevent the highly non-convex optimization from collapsing into local minima, the initial spatial coordinates and intensities of the Gaussian primitives are probabilistically sampled from a preliminary OSEM reconstruction, where the latter is further modulated by a scaling factor  $k$  to align the initial energy distribution. (iii) Adaptive densification control. Accurate capture of complex sub-centimeter morphologies is achieved through an adaptive cloning and splitting mechanism triggered by positional gradient thresholds.

## 2.2 Guided Multi-Modal Kernel Prior

To mitigate overfitting to Poisson noise and morphological collapse in ill-posed low-count PET, we regularize 3DGS optimization via a hybrid multi-modal kernel prior. For each voxel  $i$ , we extract localized patch features  $\mathbf{f}_i^P$  and  $\mathbf{f}_i^M$  from PET and co-registered MRI, respectively. To adaptively fuse functional and structural cues, we derive a voxel-wise reliability weight  $\rho_i \propto \max(0, \text{SSIM}_i - C)$

based on their local structural similarity. The affinity  $w_{i,j}$  between voxel  $i$  and its  $k$ -nearest neighbors is formulated via a confidence-weighted distance  $D_{i,j}$ :

$$w_{i,j} = \exp\left(-\frac{D_{i,j}}{N_f \sigma^2}\right), \quad D_{i,j} = \frac{\bar{\rho}_{ij}^P \|\mathbf{f}_i^P - \mathbf{f}_j^P\|_2^2 + 3\bar{\rho}_{ij}^M \|\mathbf{f}_i^M - \mathbf{f}_j^M\|_2^2}{\bar{\rho}_{ij}^P + 3\bar{\rho}_{ij}^M} \quad (4)$$

where  $\bar{\rho}_{ij}^P = (1-\rho_i)(1-\rho_j)$  and  $\bar{\rho}_{ij}^M = \rho_i \rho_j$  dynamically balance the modality contributions, preventing artifact propagation in unmatched regions. These weights form a sparse, row-normalized affinity matrix  $\mathbf{K}$ . By mapping the Gaussian-parameterized tracer distribution  $\mathbf{x}(\Theta)$  via  $\mathbf{x}_{out} = \mathbf{K}\mathbf{x}(\Theta)$ ,  $\mathbf{K}$  acts as a modality-aware projection operator.

### 2.3 Synergistic Optimization

To jointly optimize the learnable Gaussian attributes  $\Theta$ , we minimize a composite objective function that couples the negative Poisson log-likelihood:

$$\min_{\Theta} \mathcal{L}(\Theta) = \sum_{m=1}^M (\bar{y}_m - y_m \ln \bar{y}_m) + \lambda \|\nabla(\mathbf{K}\mathbf{x}(\Theta))\|_1 \quad (5)$$

Here,  $y_m$  and  $\bar{y}_m$  represent the measured and expected projection data, respectively, and  $\lambda$  governs the regularization strength. While the explicit Gaussian primitives retain the spatial agility required for complex morphologies, the MRI/CT-guided matrix  $\mathbf{K}$  enforces cross-modal anatomical consistency.

## 3 Experiments and Results

### 3.1 Data

**Brain Data Simulation.** The BrainWeb phantom [2] was utilized to simulate 3D  $^{18}\text{F}$ -FDG PET images and paired MRI images. The image dimensions were  $128 \times 128 \times 96$  with  $2 \times 2 \times 2 \text{ mm}^3$  voxel size. Eight randomly located lesions (radii: 2–8 mm) generated. 200 ps timing resolution was employed. The system matrix was computed using the Joseph3D algorithm in the PyTomography library, yielding sinograms of size  $224 \times 449 \times 4096$ .

**Real clinical Data.** The proposed framework was validated on real clinical TOF-PET/CT studies retrospectively collected from routine oncology examinations at the hospital. All patients underwent whole-body PET/CT scans following the intravenous injection of  $^{18}\text{F}$ -FDG. To address GPU memory constraints, original PET  $2.1 \times 2.1 \times 2.1 \text{ mm}^3$  and CT  $0.875 \times 0.875 \times 1.5 \text{ mm}^3$  volumes were pre-processed and cropped to  $128 \times 128 \times 96$  voxels.

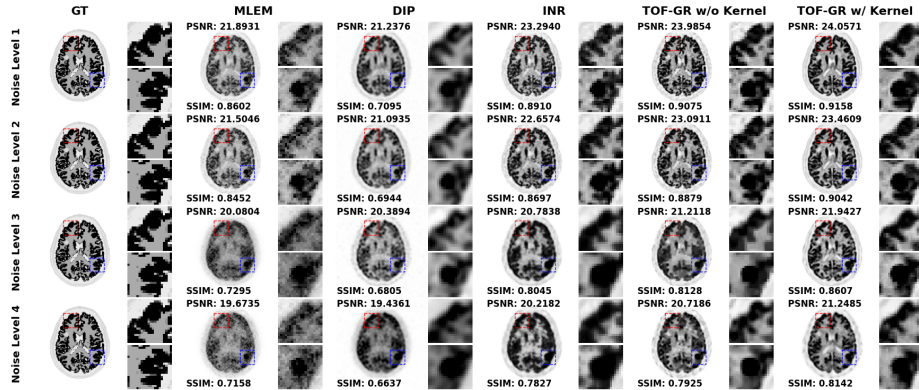


Fig. 2: Visual comparison of the reconstruction results for MLEM, DIP, INR, and proposed TOF-GR on simulated brain data

Table 1: Quantitative comparison of PET reconstruction performance across four noise levels.

| Method            | PSNR (dB) $\uparrow$ |              |              |              | SSIM $\uparrow$ |               |               |               |
|-------------------|----------------------|--------------|--------------|--------------|-----------------|---------------|---------------|---------------|
|                   | 1e8                  | 5e7          | 1e7          | 5e6          | 1e8             | 5e7           | 1e7           | 5e6           |
| MLEM              | 22.44                | 20.24        | 19.45        | 18.89        | 0.8699          | 0.8123        | 0.7484        | 0.7292        |
| DIP               | 21.72                | 21.02        | 21.58        | 22.19        | 0.6027          | 0.6964        | 0.6814        | 0.6526        |
| INR               | 24.12                | 23.27        | 23.09        | 22.76        | 0.8995          | 0.8816        | 0.8561        | 0.8450        |
| TOF-GR w/o Kernel | 26.12                | 25.29        | 23.48        | 22.93        | 0.9286          | 0.9164        | 0.8667        | 0.8386        |
| TOF-GR w/ Kernel  | <b>26.29</b>         | <b>25.72</b> | <b>24.20</b> | <b>23.43</b> | <b>0.9423</b>   | <b>0.9326</b> | <b>0.8956</b> | <b>0.8633</b> |

**Implementation Details.** The proposed 3D reconstruction framework was implemented in PyTorch and deployed on a single NVIDIA V100 GPU with 32 GB of memory. The Adam optimizer was utilized with a learning rate of  $5 \times 10^{-4}$ , while the learning rates for position, scale, rotation, and intensity parameters were configured at 0.005, 0.01, 0.001, and 0.005, respectively. In addition, this study calculated two quantitative metrics: the structural similarity index measure (SSIM) and peak signal-to-noise ratio (PSNR). To rigorously quantify the fidelity of subtle lesion recovery, we employ the Contrast Recovery Coefficient (CRC) and background standard deviation (SD). Furthermore, for clinical patient data we use the Contrast-to-Noise Ratio (CNR) and  $SUV_{max}$  to evaluate the detectability of lesions.

**Baseline.** Various baseline methods were compared with our proposed unsupervised framework: Maximum Likelihood Expectation Maximization (MLEM) [23] is a classic traditional reconstruction algorithm. Deep Image Prior (DIP) [25] represents a standard unsupervised deep learning paradigm. Implicit Neural Representation (INR) [18] utilizes a Multilayer Perceptron (MLP) to fit the map-

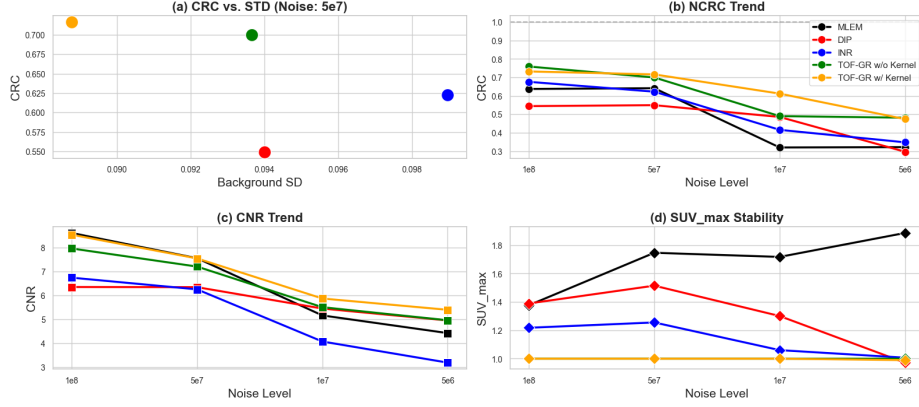


Fig. 3: Quantitative performance comparison of reconstruction methods across multiple noise levels. (a) CRC vs. STD scatter plot at  $5 \times 10^7$  counts, showing the trade-off between contrast recovery and background noise. (b) Normalized CRC (NCRC) trends across four noise levels, evaluating contrast recovery accuracy. (c) CNR curves, indicating lesion detectability. (d)  $SUV_{max}$  stability curves, illustrating the consistency of peak uptake recovery under varying noise conditions.

ping from spatial coordinates to image intensities as an implicit representation method.

### 3.2 Results

**Results on Simulation Data.** Fig. 2 demonstrates that our TOF-GR method consistently outperforms MLEM, DIP, and INR across all count levels ( $5 \times 10^6$  to  $10^8$ ). TOF-GR effectively recovers intricate anatomical boundaries and sub-centimeter tumors, where baseline methods exhibit noise-induced blurring. Ablation results confirm the Kernel module’s role in enhancing local feature representation and anatomical fidelity via Gaussian-parameterized manifolds.

As shown in Fig. 3, TOF-GR achieves a superior bias-variance trade-off. While baseline methods suffer from severe contrast degradation under photon starvation, TOF-GR’s explicit spatial parameterization preserves high-frequency lesion boundaries against over-smoothing. Furthermore, NCRC and CNR curves highlight our method’s superior stability and noise resilience. Unlike the erratic  $SUV_{max}$  fluctuations in MLEM and DIP, which suggest poor convergence in ill-posed scenarios, our framework ensures accurate quantification and robustness even under extreme noise, facilitating reliable low-dose imaging.

**Results on clinical Data.** Fig. 4 compares clinical reconstructions. MLEM exhibits excessive noise, while DIP introduces over-smoothing artifacts that compromise lesion fidelity. Although INR achieves better balance, TOF-GR demonstrates superior edge sharpness and the highest CNR. Specifically, integrating the

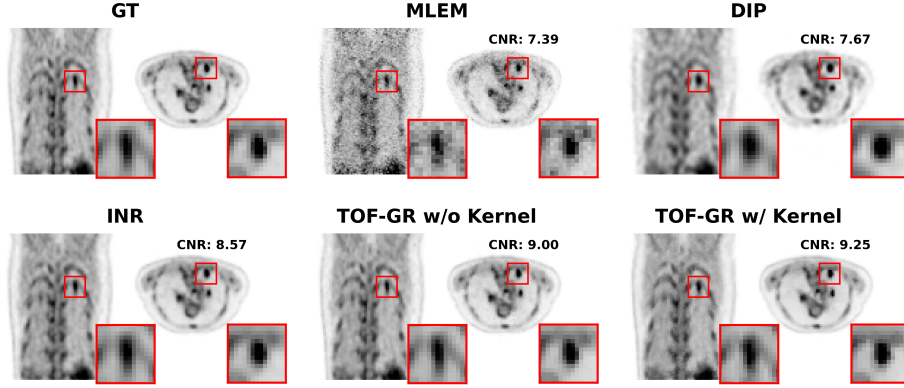


Fig. 4: Qualitative assessment of clinical PET image quality and Contrast-to-Noise Ratio (CNR).

Table 2: Ablation study and parameter sensitivity analysis. Left: Results of TOF-GR w/o Kernel for  $\lambda$  and  $k$ . Right: Results of the full TOF-GR w/ Kernel framework for  $\lambda$  and  $k$ .

| TOF-GR w/o Kernel |                  |                 |                 | TOF-GR w/ Kernel |                  |                 |                 |
|-------------------|------------------|-----------------|-----------------|------------------|------------------|-----------------|-----------------|
| Method            | Parameters       | PSNR $\uparrow$ | SSIM $\uparrow$ | Method           | Parameters       | PSNR $\uparrow$ | SSIM $\uparrow$ |
| TOF-GR w/o Kernel | $\lambda = 0.01$ | 24.81           | 0.9437          | TOF-GR w/ Kernel | $\lambda = 0.01$ | <b>25.57</b>    | <b>0.9519</b>   |
|                   | $\lambda = 0.05$ | 25.09           | 0.9469          |                  | $\lambda = 0.05$ | 25.52           | 0.951           |
|                   | $\lambda = 0.10$ | <b>25.29</b>    | <b>0.9488</b>   |                  | $\lambda = 0.10$ | 25.38           | 0.9489          |
|                   | $\lambda = 0.50$ | 23.93           | 0.9266          |                  | $\lambda = 0.50$ | 23.91           | 0.9259          |
| TOF-GR w/o Kernel | $k = 0.20$       | 24.57           | 0.9380          | TOF-GR w/ Kernel | $k = 0.20$       | 24.69           | 0.9402          |
|                   | $k = 0.50$       | <b>25.29</b>    | <b>0.9488</b>   |                  | $k = 0.50$       | 25.52           | 0.9513          |
|                   | $k = 0.80$       | 25.19           | 0.9477          |                  | $k = 0.80$       | <b>25.57</b>    | <b>0.9519</b>   |

Anatomical Kernel Prior further sharpens boundaries and significantly enhances tumor contrast, effectively recovering structural details even in challenging clinical scenarios.

**Ablation Studies.** Sensitivity analysis in Table 2 underscores the intrinsic stability of our framework. While the baseline TOF-GR performance fluctuates with parameter tuning, TOF-GR w/ Kernel maintains a uniformly higher performance floor across varying regularization coefficients and scaling factors. This demonstrates that the Anatomical Kernel Prior not only enhances peak reconstruction accuracy but also significantly mitigates hyperparameter sensitivity, ensuring robust convergence and practical reliability in clinical settings.

## 4 Discussion and Conclusion

TOF-GR demonstrates significant potential, yet several frontiers remain for enhancement. Extending the 3D Gaussian primitives to 4D temporal modeling would allow the framework to capture dynamic kinetic distributions. Integrating parametric imaging could further unveil underlying physiological changes. Additionally, changing the projection could further boost resolution. These advancements will broaden TOF-GR’s applicability in multi-parametric clinical protocols.

We presented TOF-GR, the first unsupervised PET reconstruction framework leveraging 3D Gaussian Splatting. By replacing grids with explicit primitives, TOF-GR resolves the bias-variance trade-off and preserves sub-centimeter details under extreme noise. Our method consistently outperforms state-of-the-art baselines, offering a robust and dose-efficient solution for clinical diagnostics.

**Disclosure of Interests.** The authors have no competing interests to declare that are relevant to the content of this article.

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